BIOSTATISTICS WITH R

SUMMER WORKSHOP (MITGEST network)

24-27 JULY 2024

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WORKSHOP SCHEDULE

- 4 days
 - 1. Intro to R and data analysis
 - 2. Statistical inference & hypothesis testing
 - 3. Modeling correlation and regression
 - 4. Machine Learning; MetaboAnalyst; Power Analysis
- Each day will include:
 - Frontal class (MORNING)
 - Practical training with R about the topics discussed in the morning. (AFTERNOON)



DAY 4 – LECTURE OUTLINE

- Examples of Machine Learning
 - PCA
 - PLS-DA
- MetaboAnalyst
 - Overview
 - Workflow
- Power analysis
 - Hypothesis testing
 - Decision errors
 - Statistical power
 - Effect size



Principal Component Analysis (PCA)

A type of *unsupervised* learning algorithm for dimensionality reduction



Purpose of PCA

•The goal of PCA is to transform a high-dimensional dataset into a lower-dimensional dataset while retaining as much of the variance in the data as possible.

•Common use cases of PCA:

- 1. to reduce the dimensionality of high-dimensional datasets
- 2. to visualize the structure of the data
- 3. to remove noise and redundant information from the data
- 4. as a preprocessing step for other machine learning algorithms



Covariance

Population mean is unknown

$$var(x) = \frac{\sum_{i}^{n} (x_{i} - \overline{x})^{2}}{N - 1} \xrightarrow{\times} y \xrightarrow{z} \left[\begin{array}{ccc} x & y & z \\ var(x) & cov(x, y) & cov(x, z) \\ v & cov(x, y) & var(y) & cov(y, z) \\ z & cov(x, z) & cov(y, z) & var(z) \end{array} \right]$$

$$cov(x,y) = rac{\sum_i^n (x_i - \overline{x}) \cdot (y_i - \overline{y})}{N-1}$$

Variance measures how the values vary in a variable. Covariance measures how changes in one variable are associated with changes in a second variable.



Covariance



Positive, negative and zero covariance.



Different variances and zero covariance.

Source: https://builtin.com/data-science/covariance-matrix



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PCA

PCA originally is a <u>linear algebra operation</u>.

It is a transformation method that creates (weighted <u>linear</u>) combinations of the original variables in a data set, with the intent that the new combinations will capture as much <u>variance</u> in the dataset as possible while eliminating correlations (i.e., redundancy).

PCA creates the new variables using the eigenvectors and eigenvalues calculated from the <u>covariance matrix</u> of your original variables.



Eigenvectors & Eigenvalues

In the context of PCA

- The **eigenvectors** of the covariance matrix define the directions of the principal components calculated by PCA.
- The **eigenvalues** associated with the eigenvectors describe the variance along the new axis.



Source: https://towardsdatascience.com/tidying-up-with-pca-an-introduction-to-principal-components-analysis-f876599af383



Principal components



Principal Component 1 accounts for variance from both variables A and B. (dimension reduction)

The principal components (eigenvectors) are sorted by descending eigenvalue. The principal components with the highest eigenvalues are "picked first" as principal components because they account for the most variance in the data.

Source: https://towardsdatascience.com/tidying-up-with-pca-an-introduction-to-principal-components-analysis-f876599af383



Principal components



To convert our original points, we create a projection matrix.

This projection matrix is just the selected eigenvectors concatenated to a matrix. We can then multiply the matrix of our original observations and variables by our projection matrix.

The output of this process is a transformed data set, projected into our new data space — made up of our principal components!

Source: <u>https://towardsdatascience.com/tidying-up-with-pca-an-introduction-to-principal-components-analysis-f876599af383</u>



PLS Discriminant Analysis (PLS-DA)

A *supervised* alternative to PCA performing simultaneous dimensionality reduction and classification



Purpose: PLS-DA vs PCA

- PCA is completely unsupervised (i.e. you don't know in advance if there are classes in your dataset)
- In PLS-DA you know how your dataset is divided in classes from the response vector Y. The goal here is then to project the predictors into a space, while maximizing the
- Common scenarios for using PLS-DA: omics sciences.



Scores plot: PCA vs PLS-DA





Samples projected in the space of Principal Components

Samples projected in the space of latent variables (components) that maximize the separation between groups

Source: Test data (**NMR spectral bins**) provided by METABOANALYST platform: https://www.metaboanalyst.ca



Loadings plot: PCA vs PLS-DA





The loading vectors (here shown as points) represent the original variables in the space PCs.

The loading vectors (here shown as points) represent the original variables in the space of latent components retrieved by PLS-DA.

Source: Test data (**NMR spectral bins**) provided by METABOANALYST platform: https://www.metaboanalyst.ca



Feature Importance in PLS-DA



VIP (Variable Importance in Projection) scores, ranking the variables based on their significance in the PLS-DA **model of classification**.

...very useful to select potential biomarkers!

Source: Test data (**NMR spectral bins**) provided by METABOANALYST platform:



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Cross validation in PLS-DA



PLS-DA generate a model of classification.

By partitioning the dataset and iteratively testing the model, cross validation estimate the predictive ability of the model.

Q² is an analogous of R² in regression: the higher the better!

Source: Test data (**NMR spectral bins**) *provided by METABOANALYST platform:*



Permutation in PLS-DA



Permutation testing is a nonparametric approach to assess the significance of a model's results.

In the context of PLS-DA, this test helps verify whether the observed classification accuracy is better than what would be expected by chance.

Test data (**NMR spectral bins**) provided by METABOANALYST platform: https://www.metaboanalyst.ca



DAY 4 – LECTURE OUTLINE

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 - 3. Statistical power
 - 4. Effect size



MetaboAnalyst

An R-driven Software



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Introduction to MetaboAnalyst



https://www.metaboanalyst.ca

From raw spectra to biomarkers, patterns, functions and systems biology

- it is a free web-based platform
- it works with **R** but it has a *friendlier* GUI: anyone can make metabolomics data analysis, interpretation and integration with other omics data
- the whole metabolomics community uses it!!!

...but

•you need a statistical background to interpret the **MetaboAnalyst** outputs and to get the most of it!



MetaboAnalyst overview



Source: Xia, J., Wishart, D. Nat Protoc 6, 743–760 (2011).



MetaboAnalyst workflow 1) data upload



Test data 1:

Binned 1H NMR spectra of 50 urine samples using 0.04 ppm constant width (<u>Psihogios NG, et al.</u>) Group 1- control; Group 2 - severe kidney disease.

Data Integrity Check:

- · Checking sample names spaces will replaced with underscore, and special characters will be removed;
- Checking the class labels at least three replicates are required in each class.
- · The data (except class labels) must not contain non-numeric values.
- If the samples are paired, the pair labels must conform to the specified format.
- · The presence of missing values or features with constant values (i.e. all zeros).

Data processing information: Checking data content ...passed. Samples are in rows and features in columns The uploaded file is in comma separated values (.csv) format. The uploaded data file contains 50 (samples) by 200 (spectra bins) data matrix. Samples are not paired. 2 groups were detected in samples. Only English letters, numbers, underscore, hyphen and forward slash (/) are allowed. Other special characters or punctuations (if any) will be stripped off. All data values are numeric. A total of 0 (0%) missing values were detected. By default, missing values will be replaced by 1/5 of min positive values of their corresponding variables Click the Proceed button if you accept the default practice; Or click the Missing Values button to use other methods. **Edit Groups** Proceed



MetaboAnalyst workflow 2) data filtering

Upload V Processing Data check Missing value Data filter Data editor Normalization Statistics Download Exit

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Data Filtering:

The purpose of the data filtering is to identify and remove variables that are unlikely to be of use when modeling the data. No phenotype information are used in the filtering process, so the result can be used with any downstream analysis. This step is strongly recommended for untargeted metabolomics datasets (i.e. spectral binning data, peak lists) with large number of variables, many of them are from baseline noises. Filtering can usually improve the results. For details, please refer to the paper by <u>Hackstadt, et al</u>.

Non-informative variables can be characterized in three groups: 1) variables that show **low repeatability** - this can be measured using QC samples using the relative standard deviation(RSD = SD/mean). Features with high percent RSD should be removed from the subsequent analysis (the suggested threshold is 20% for LC-MS and 30% for GC-MS); 2) variables that are **near-constant** throughout the experiment conditions - these variables can be detected using standard deviation (SD); or the robust estimate such as interquantile range (IQR); and 3) variables of **very small values** (close to baseline or detection limit) - these variables can be detected using mean or median.

For data filtering based on the last two categories, the default parameters follow the empirical rules: 1) Less than 250 variables: 5% will be filtered; 2) Between 250 - 500 variables: 10% will be filtered; 3) Between 500 - 1000 variables: 25% will be filtered; and 4) Over 1000 variables: 40% will be filtered. You can turn off data filtering by dragging the slider to adjust the percentage to filter out to be 0, when your data contain less than 5000 features (or 2500 for power analysis) to control computing time on our server.

Reliability filter:	Filtering features based on technical repeatability QC samples	RSDs greater than:
Variance filter:	 Interquantile range (IQR) Standard deviation (SD) Median absolute deviation (MAD) Relative standard deviation (RSD = SD/mean) Non-parametric relative standard deviation (MAD/median) 	Percentage to filter out:
Abundance filter:	 Mean intensity value Median intensity value 	Percentage to filter out:
	Submit	Proceed



MetaboAnalyst workflow 3) data normalization

Normalization (

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Data check

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Normalization Overview:

The normalization procedures are grouped into three categories. You can use one or combine them to achieve better results.

- Sample normalization is for general-purpose adjustment for systematic differences among samples;
- Data transformation applies a mathematical transformation on individual values themselves. A simple mathematical approach is used to deal with negative values in log and square root Please search OmicsForum using "normalization #metaboanalyst" to find more information.
- Data scaling adjusts each variable/feature by a scaling factor computed based on the dispersion of the variable.

Sample normalization	
None	
Sample-specific normalization (i.e. weight, volume) Specify	
O Normalization by sum	
Normalization by median	
Normalization by a reference sample (PQN) Specify	
Normalization by a pooled sample from group (group PQN) Specify	
Normalization by reference feature Specify	
Quantile normalization (suggested only for > 1000 features)	
Data transformation	
O None	Autoscoling
Log transformation (base 10)	Autoscanng
Square root transformation (square root of data values)	
Cube root transformation (cube root of data values)	
Data scaling	
None	D I I
Mean centering (mean-centered only)	Pareto scaling
Auto scaling (mean-centered and divided by the standard deviation of each variable)	
O Pareto scaling (mean-centered and divided by the square root of the standard deviation of each variable)	
Range scaling (mean-centered and divided by the range of each variable)	
	a.
Normalize View Result Proceed	



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MetaboAnalyst workflow 3) data normalization





After Normalization

Before Normalization

Effect of normalization over sample





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MetaboAnalyst workflow 3) data normalization

Effect of features/metabo scaling





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MetaboAnalyst workflow 4) statistical analysis



«Classical» analysis of variance among groups

Machine learning algorithms



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MetaboAnalyst workflow 4) univariate analysis

Show R Commands

Two-sample t-tests & Wilcoxon rank-sum tests

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For large data set (> 1000 variables), both the paired information and the group variance will be ignored, and the default parameters will be used for t-tests to save computational time. If you choose non-parametric tests (Wilcoxon rank-sum test), the group variance will be ignored.

Analysis type:	Unpaired 🗸
Group variance:	Equal 🗸
Non-parametric tests:	
P-value threshold:	0.05 Raw O FDR





MetaboAnalyst workflow 4) univariate analysis

Volcano Plot

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> K-means RandomFor SVM Download Exit

Volcano plot combines results from Fold Change (FC) Analysis and T-tests into one single graph which allows users to intuitively select significant features based on either biological significance, statistical significance, or both. Please refer to the Fold change and T-test web pages for details of the underlying calculations.

Data check					
Missing valu	Analysis:	Unpaired			
Data filter	Plot style:	Theme: 🔵 Blackwh	ite 🔾 Grey 🚫 Minimal 🚫 Classic		
Data editor	(for download image)	Labeling: 🔿 All signi	ficant O Top N 5		
Normalization					
Statistics		Fold change (FC)	2.0 (min value is 1 indicating no		
Fold change	X-axis:	threshold:	change)	Submit	
T-test		Direction of	patient/control 🗸		
Volcano plot		comparison.			
ANOVA		Non-parametric tests			
Correlations	Y-axis:	P-value threshold:	0.1 O Raw O FDR		
DSPC netwo		Group variance:	Foual		
PatternHunt			Equal		
PCA					
PLSDA	Click a point to v	iew; drag to zoom; rese	et zoom at bottom		
SPLSDA	9				Sig.Down [6]
OrthoPLSDA					
SAM	8	0			
EBAM					
Dendrogram	7				
Heatmap		0	•		9
SOM	6				0











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Hierarchical Clustering Heatmaps

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A heatmap provides intuitive visualization of a data table. Each colored cell on the map corresponds to a concentration value in your data table, with samples in rows and features/compounds in columns. You can use a heatmap to identify samples/features that are unusually high/low. The maximum number of features can be displayed is 2000 features (selected based on IQR by default). You can use Select features for better control



Heatmap of the top 25 T-test features



Identifying the metabolic pathways deregulated by a pathology is finding a target for pharmacological therapy!



Source: https://www.behance.net/gallery/38270165/Metro-Map-of-Metabolism-The-Overview



MetaboAnalyst workflow 6) enrichment analysis

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	Data check
	Name check
	Missing value
	Data filter
	Data editor
	Normalization
>	Enrichment
	Download

Test data 2: Urinary metabolite concentrations from 77 cancer patients measured by 1H NMR. Phenotype:

- N cancer cachexic;
- Y control



Data Integrity Check:

· Checking sample names - spaces will replaced with underscore, and special characters will be removed;

- · Checking the class labels at least three replicates are required in each class.
- · The data (except class labels) must not contain non-numeric values.
- · If the samples are paired, the pair labels must conform to the specified format.
- The presence of missing values or features with constant values (i.e. all zeros).

	Data processing information:
Checki	ng data contentpassed.
Sample	es are in rows and features in columns
The up	loaded file is in comma separated values (.csv) format.
The up	loaded data file contains 77 (samples) by 63 (compounds) data matrix.
Sample	es are not paired.
2 group	os were detected in samples.
Only Er	nglish letters, numbers, underscore, hyphen and forward slash (/) are allowed.
Other s	special characters or punctuations (if any) will be stripped off.
All data	a values are numeric.
A total	of 0 (0%) missing values were detected.
<u>By defa</u>	ault, missing values will be replaced by 1/5 of min positive values of their corresponding variables
Click th	ne Proceed button if you accept the default practice;
Or click	K the Missing Values button to use other methods.

MetaboAnalyst workflow 6) enrichment analysis

Name/ID Standardization:

tool in Other Utilities module;

Image: Definition of the second secon

 Greek alphabets are not recognized, they should be replaced by Englis Query names in normal white indicate exact match - marked by "1" in ti Query names highlighted indicate no exact or unique match - marked For compound name, you should click the View link to perform approx For KEGG ID, it is possible to have multiple hits, you should click the View 			
Query	Hit		
1,6-Anhydro-beta-D-glucose	Levoglucosan		
1-Methylnicotinamide	1-Methylnicotinamic		
2-Aminobutyrate	L-alpha-Aminobutyr		
2-Hydroxyisobutyrate	2-Hydroxyisobutyra		
2-Oxoglutarate	Oxoglutaric acid		
3-Aminoisobutyrate	3-Aminoisobutanoic		
3-Hydroxybutyrate			
3-Hydroxyisovalerate	3-Hydroxyisovaleric		
3-Indoxylsulfate	Indoxyl sulfate		
4-Hydroxyphenylacetate	p-Hydroxyphenylac		
Acetate	Acetic acid		
Acetone	Acetone		

· For enrichment analysis, only well-annotated HMDB compounds (i.e. th

Nan	ne ma	atch				×	d ID Conversion
		Matched Name	НМДВ	PubChem	KEGG		
		3- Hydroxyisovaleric acid	HMDB0000754	<u>69362</u>	<u>C20827</u>		
		3-Hydroxybutyric acid	HMDB0000011	<u>441</u>	<u>C01089</u>		Details
		(S)-3- Hydroxybutyric acid	HMDB0000442	<u>94318</u>	<u>C03197</u>		
		Ethyl (±)-3- hydroxybutyrate	HMDB0040409	<u>62572</u>	NA		
		Methyl 3- hydroxybutyrate	HMDB0041603	<u>15146</u>	NA		
		L-Threonine	HMDB0000167	<u>6288</u>	<u>C00188</u>		'iew
		4-Amino-3- hydroxybutyrate	HMDB0061877	<u>2149</u>	<u>C03678</u>		
		2-Methyl-3- hydroxybutyric acid	HMDB0000354	<u>160471</u>	NA		
		None of the above					
		ок		Cancel			



Adipate Alanine

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Adipic acid

Alanine

MetaboAnalyst workflow 6) enrichment analysis

Parameter Setting

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Data check

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Enrichment tests are based on the well-established globaltest to test associations between metabolite sets and the outcome. The algorithm uses a generalized linear model to compute a 'Q-stat' for each metabolite set. The Q-stat is calculated as the average of the Q values calculated for the each single metabolites; while the Q value is the squared covariance between the metabolite and the outcome. The globaltest has been shown to exhibit similar or superior performance when tested against several other popular methods.

Metabolite sets: Unlike transcriptomics which allows comprehensive gene expression profiling, targeted metabolomics usually covers only a small percentage of metabolome (the actual coverage is platform/protocol specific). This means that metabolites (defined in our current pathways or metabolite sets) do not have equal probabilities of being measured in your studies, and the enriched functions are the results from both platform/protocol specific effects and biological perturbations. Since the primary interest is to detect the latter, we highly recommend uploading a reference metabolome containing all measurable metabolites from your platform to eliminate the former effects

Data filter	Please select a metabo	lite set library	
Data editor			
lormalization		SMPDB	99 metabolite sets based on normal human metabolic pathways.
nrichment	ichment		80 metabolite sets based on KEGG human metabolic pathways (Dec. 2023).
View result	Pathway based	Orug related	461 metabolite sets based on drug pathways from SMPDB.
ownload		RaMP-DB	3694 metabolite and lipid pathways from RaMP-DB
kit			(integrating KEGG via HMDB, Reactome, wikiPathways).
		OBlood	480 metabolite sets reported in human blood.
	Disease	OUrine	385 metabolite sets reported in human urine.
	signatures	⊖ CSF	174 metabolite sets reported in human cerebral spinal fluid (CSF).
		⊖ Feces	67 metabolite sets reported in human feces.
Chemcial		Super-	39 super chemical class metabolite sets or lipid sets
	structures	O Main-class	617 main chemical class metabolite sets or lipid sets
		Sub-class	1250 sub chemical class metabolite sets or lipid sets
		⊖ SNPs	4,598 metabolite sets based on their associations with SNPs loci.
	Other types	OPredicted	912 metabolic sets predicted to change in the case of dysfunctional enzymes.
		OLocations	78 metabolite and lipid sets based on organ, tissue, and subcellular localizations.
		CExposure	62 metabolite sets based on dietary and chemical exposures.
	Self defined	O Upload here	define your own customized metabolite sets
	Only use metabolite	sets containing a	it least 2 entries 🗸
	Please specify a refere	nce metabolom	9
	O Use all the compo	unds in the selec	ted library

Upload a reference metabolome based on your analytical platform

Enrichment analysis, based on the globaltest, tests associations between metabolite sets and the outcome. The algorithm uses a generalized linear model to compute a 'Q-stat' for each metabolite set.



MetaboAnalyst workflow 6) enrichment analysis





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MetaboAnalyst workflow 6) functional interpretation





MetaboAnalyst workflow

Metabolic pathway analysis and visualization



Source: Xia, J., Wishart, D. Nat Protoc 6, 743–760 (2011).



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Hypothesis testing steps

- 1. State the hypotheses (the null hypothesis and an alternative hypothesis)
- 2. Design the analysis (*e.g.* the significance level is 0.05, the test method one-sample z-test)
- 3. Analyze sample data
- 4. Interpret result and make decision



What are the Null and Alternative hypotheses?

Null Hypothesis	Alternative Hypothesis or
 is the hypothesis that a sample data statistic occurs purely from chance e.g. there is no difference between the mean pulse rate for people doing physical exercise and the normal pulse rate 	 is the hypothesis that a sample data statistic is influenced by some non-random cause e.g. the mean pulse rate for persons doing the physical exercise is higher than the normal
 Must contain condition of equality , Test the Null Hypothesis directly: reject or fail to reject 	 Must be true if is false (corresponding to , conditions) `opposite' of Null Hypothesis



Decision Errors

Two types of errors can result from a hypothesis test.

- Type I error occurs when the researcher rejects a null hypothesis when it is true. The probability of committing a Type I error is called the significance level. This probability is also called alpha, and is often denoted by α.
- Type II error occurs when the researcher fails to reject a null hypothesis that is false. The probability of committing a Type II error is called Beta, and is often denoted by β. The probability of not committing a Type II error is called the Power of the test.



Summarizing Type I and Type II Errors



Which is worse: false-positive or falsenegative?

	Fail to reject H0	Reject H0
H0 is true	TRUE NEGATIVE	FALSE POSITIVE
probability	1- <i>a</i>	α
H1 is true	FALSE NEGATIVE	TRUE POSITIVE
probability	β	power = 1- β

Example 1. Covid-19 test: • Fals Example 2. Quality control in a pharma production alth company qua Fals . Fals Example 3. Disease diagnosis . pres We have Fals shel • Example 3. Criminal court of d cent. Fals was . as a False-POSITIVE: an innocent citizen is found guilty Fals defe • and is sent to prison or receives the death penalty the prov. False-NEGATIVE: a criminal is declared innocent fatal and escapes punishment



Controlling Type I and Type II Errors

- α , β , and **n** are related
- when two of the three are chosen, the third is determined
- usually the researcher fix the type I error (α) he can tolerate before experiment and then compare the p-value and takes a decision



Controlling Type I and Type II error



p-value

The p-value corresponds to the answer the question: what is the probability of the observed test statistic or one more extreme when H0 is true?





p-value interpretation



- A very small p-value means that such an extreme observed <u>outcome</u> would be very unlikely under the null hypothesis.
- Usually the researcher fix α before experiment and then compare the p-value and takes a decision.

Conventions

P > 0.10	\Rightarrow
$0.05 < P \le 0.10$	\Rightarrow
$0.01 < P \le 0.05$	\Rightarrow
<i>P</i> ≤ 0.01	\Rightarrow

- non-significant evidence against H0
 - marginally significant evidence against H0
 - significant evidence against H0
 - highly significant evidence against H0



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	Fail to reject H0	Reject H0		
H0 is true	Correct action	Type I error FALSE POSITIVE		
probability	1-α	α		
H1 is true	Type II error FALSE NEGATIVE	Correct action		
probability	β	power = 1- β		

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1) Raise significance level alpha (the WRONG way)





2) Switch from a 2-tailed test to a 1-tailed test (CORRECT if possible)





3) Increase mean difference (or increase the effect size)





4) Use z distribution instead of t distribution (appropriate when we know the population mean)





5) Decrease standard deviation (using more precise measurements to have less error and less noise)





6) Increase sample size (the most practical way)





The effect size is an estimate of the difference between two or more groups.

The measurement of the effect size depends on the type of analysis your are doing:

1. Studying the mean difference between two groups In this case you use a standardized mean difference (Cohen's *d*)









2) Pearson Correlation Coefficient: measuring the linear association between two variables X and Y.

- -1 = perfectly negative linear correlation between two variables
- 0 = no linear correlation between two variables
- 1 = perfectly positive linear correlation between two variables



Source: https://www.statology.org/effect-size/



Pearson Correlation Coefficient

r	Effect size
0.1	small
0.3	medium
>0.5	large



Effect size in different scenarios

Test	Effect Size	Small	Medium	Large
 All t-tests: one-sample t-test independent samples t-test paired samples t-test 	Cohen's d d =	0.20	0.50	0.80
Difference between many means (ANOVA)	Cohen's f f =	0.10	0.25	0.40
Chi-squared test	Cohen's w	0.10	0.30	0.50
Pearson's correlation coefficient	Pearson's	0.10	0.30	0.50
Linear Regression (entire model)	Cohen's	0.02	0.15	0.35

Source: https://en.wikipedia.org/wiki/Effect_size#Overview

